

Significant Figures Enriched Notes

Which digits are significant?

- **Rule #1:** All non-zero digits are significant.
24 has two sig figs, 24.1 has 3 sig figs
- **Rule #2:** All zeros bounded by non-zero integers are significant.
2004 has four sig figs 20.04 also has 4 sig figs
- **Rule #3:** Zeros placed before other digits (leading zeros) are not significant.
0.024 has 2 sig figs
- **Rule #4:** Zeros at the end of a number are significant ONLY if they come after a decimal point.
2.40 has three sig figs 240 only has 2 sig figs

Practice:

409.25	0.050	0.003500
83	300 900	0.916
98.207	4.67×10^{-7}	0.200
0.001	45.030	5 234 000
4.3×10^2	35 000	150 000 001
0.003050	0.004400	460 090
4 200	16.8090	50.00300

Rules for Addition and Subtraction

- Answers must be rounded to the **same decimal place** (not sig figs) as the **least** number of decimal places in any of the numbers being added or subtracted.

Ex. $2.42 + 14.2 + 0.6642 = 17.2842$ becomes

- If there is no decimal point in one of the numbers, all decimal points are dropped.

Rules for Multiplication and Division

- The number of sig figs in the answer should be the same as in the number with the least sig figs being multiplied or divided.

Ex. $7.3 \times 1264 = 9227.2$ becomes

When doing multiple steps in a word problem

- Solve each step using order of operations.
- **Do not round off any number.**
- Once you have your final answer, then you use significant figures according to the last step you do.

Ex: $\frac{125 \times 345.5}{65.3 + 16.6} = \frac{43187.5}{81.9} = 527.3199023$ becomes

Exceptions and special circumstances

1. Adding and scientific notation

$$\frac{(5.8 \times 10^2) + 368}{4.87 \times 10^5}$$

- When adding and using SN, the exponents must be the same.

You have 2 options to solve the problem.

1- Convert 5.8×10^2 to 580 and get rid of the exponent

$$580 + 368$$

2- Convert 368 to the same exponent so it becomes 3.68×10^2

$$5.8 \times 10^2 + 3.68 \times 10^2$$

Both are correct, but option 1 is easier

2. Rounding off and keeping a zero as a significant digit

$$\frac{8253.0569}{12.7} = 649.847$$

- In this example you must keep 3 sig figs in your answer.

When rounding off 649.847 should become 650.

Problem, 650 only has 2 sig figs

Solution: put a – above the zero, this makes it significant.

Becomes

3. Having many insignificant zero's and addition

- When adding the following: $136.2 + 2\,500\,000 + 14.01$
We get $2\,500\,150.21$ which should become $2\,500\,150$.

EXCEPT, we have to use sig figs, and the addition rule says that we must round to the least precise decimal place. Therefore, because $2\,500\,000$ is only precise to the hundred thousands place, we need to round the answer to $2\,500\,000$.

- You cannot be more precise than your least most precise number.
This is true for any additions that end in non sig. zero's. ex-
 $5\,500 + 15 = 55\,15$ but becomes
 $310 + 6 = 316$ but becomes
 $259\,500 + 1670 + 23 = 261\,193$ but becomes

4. Converting units

- When converting units, sig figs need to be maintained.
Ex 1- 4.0 cm to m becomes 0.040 m not 0.04 m
Ex 2- 1250 mL becomes 1.25 L not 1.250 L

5. Constants

- When there is a constant in a formula, the constant does not count as a significant figure.
ex: Coulomb's constant $9.00 \times 10^9\text{ Nm}^2/\text{C}^2$

SIG FIGS PRACTICE

1. How many sig figs are in each of the following numbers?

- | | |
|-----------------------|-------------------------|
| a) 0.09304 | f) 1204.0 |
| b) 6.58×10^7 | g) 2.9×10^{-3} |
| c) 0.0200 | h) 2.4×10^7 |
| d) 0.10101 | i) 460 |
| e) 4.508 | j) 23.230 |

2. Solve using the correct number of significant figures.

a- $13.5 \times 14.2 \times 13.080 \times 0.01 = 25.07436 =$

$$\text{b- } 187 \times 0.008 \div 14.2887 = 0.104698118 =$$

$$\text{c- } 911 \times 677 \times 0.0089 = 5489.0483 =$$

$$\text{d- } 8.0 \times 10^5 \div 4.02 \times 10^9 = 0.000199005 =$$

$$\text{e- } (1.23 \times 10^5) (1.445 \times 10^7) \div 0.023 = 7.727608696 \times 10^{13} =$$